



E-ISSN: 2707-6644
 P-ISSN: 2707-6636
 IJCPDM 2022; 3(1): 23-29
 Received: 10-11-2021
 Accepted: 15-12-2021

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For fuzzy classification of databases with FCQL

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DOI: <https://doi.org/10.33545/27076636.2022.v3.i1a.36>

Abstract

Business information systems have extensive databases that are mainly managed in relational databases. What is often missing are automated procedures to analyze these inventories without major restructuring. Therefore, we extend the relational database schema with a context model for fuzzy classification. Based on this, we develop the fuzzy classification query language, FCQL, which allows fuzzy queries to the extended database schema using linguistic variables and converts them into SQL calls to the database. With this we give the user a data mining tool so that he can start extended queries on his databases based on a predefined fuzzy classification and obtain an improved basis for decision-making.

Keywords: Business, information systems, relational database, SQL, data mining

Introduction

On the way to the information society, a lack of data has turned into an overabundance (information overload). Therefore, companies and organizations are interested in tools for data analysis in order to continue to have a basis for business decisions. Of particular interest is the process of Knowledge Discovery in Databases (KDD), which extracts valuable information from sometimes extensive databases.

The primary goal of a KDD process is to reduce the complexity of the data or recognizing patterns in large databases. Classic methods such as cluster analysis or regression analysis are mostly based on statistical methods. They assume that the amounts of data or databases contain numerical values or contain sharp data values. As soon as the data itself or the classes that are defined in the data analysis and to which the data is then assigned to reduce complexity are no longer clearly defined, many conventional data analysis methods fail.

Motivation

In companies, the databases contain not only numerical data but also non-numerical information. Database query languages require queries to be formulated with the same level of detail and precision as the data is stored in the database. Relational query languages, such as SQL, do not permit imprecisely formulated or fuzzy queries.

Figure 1 illustrates a fuzzy query that uses the vague term 'unacceptable' (see Figure 3 for table example, see Figure 6 for definition of term). This small visual example illustrates the need to be able to operate with vague and imprecise queries in the case of large databases. Even in the case of fuzzy classification, there are many practical examples from everyday business.

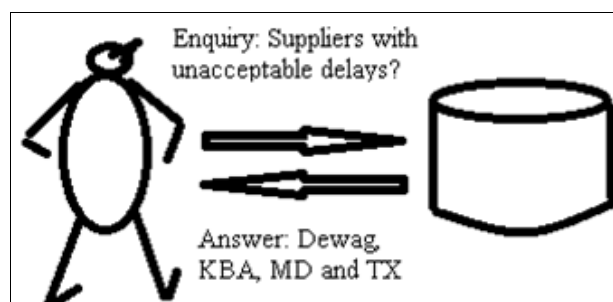


Fig 1: Fuzzy query of a relational database

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- **Customer Relationship Management:** Recently, the management of customer relationships and processes has gained in importance. In addition, the customers are happy to be based on certain characteristics resp. of purchasing behavior divided into classes or customer segments. A common division is into A, B and C customers, depending on the customer's purchasing power. In most cases, this class affiliation is strictly defined, i.e. each customer belongs to exactly one class. If the development potential is to be taken into account in addition to the completed transactions, an individual customer can no longer be clearly assigned to a customer segment. Analyzing the possibly extensive customer base and creating fuzzy customer segments is a must. This is the only way that suitable marketing, sales and after-sales service tasks can be carried out in a targeted and cost-effective manner.
- **Checking creditworthiness and risk:** Insurance companies and banks divide their customers into various classes based on risk considerations. Age, purchasing power and other characteristics must be checked for a loan application. Instead of sharp creditworthiness or risk classes, fuzzy classes that work with the help of a membership function can be interesting. Based on research, it has been found that traditional credit checks and clearly different risks can result in the same overall rating for the customer. Conversely, it is also possible that different overall ratings can arise if the customer's characteristics are very similar.
- **Selection of suppliers:** Evaluations must be made in order to select suppliers. Conventional or sharp classifications of suppliers, e.g. according to delivery date and quality characteristics, do not guarantee that a promising and long-term relationship can be maintained. The structure contained in the stored supplier data, but not visible or not yet visible, is made visible by fuzzy class formation. It allows a targeted and effective treatment of the individual supplier classes.

Business information systems generate a wealth of data. In day-to-day business, but above all to secure decisions, it is necessary to analyze these sometimes extensive data stocks or databases. Without a proper KDD process with fuzzy data analytics, you risk missing out on valuable information — both risks and opportunities.

Databases and fuzzy logic

In databases, especially in relational database systems, the characteristic values are assumed to be unique and queries to the database produce clear results. Relational databases can be characterized as follows:

- The feature values in the databases are precise, i.e. they are unique. Already in the requirement of the first normal form we require that the characteristic values are atomic and come from a well-defined range of values. Imprecise characteristic values such as a supplier's delay is "2 or 3 or 4 days" or vague characteristic values such as the delay is "approximately 3 days" are not permitted.
- The characteristic values stored in a relational database are secure, i.e. the individual values are either known or unknown. An exception are the zero values, i.e.

characteristic values that are not or not yet known. In addition, the database systems do not support us in any way in modeling an existing stochastic uncertainty. In other words, probability distributions for feature values are excluded; it remains difficult to express whether a given feature value corresponds to the true value or not.

- Queries to the database are sharp. They always have a dichotomous character, i.e. a query value given in the query must either match or not match the characteristic values in the database. An evaluation of the database in which a query value "more or less" matches the stored characteristic values is not permitted.

For several years, findings from the field of fuzzy logic have been applied to data modeling and databases, see eg Bordogna and Pasi^[1], Bosc and Kacprzyk^[2], Chen^[3], Petry^[4], Pons *et al.*^[5]. Most of this work is theoretical in nature; however, some research groups have attempted to demonstrate the usefulness of fuzzy database models and database systems with implementations.

With data modeling, a larger field of application can be opened up if incomplete, vague or imprecise facts are allowed. With the help of fuzzy logic, various model extensions were proposed, both for the entity relationship model and for the relational model. For example, in his dissertation, Chen expanded the classical normal forms of database theory into fuzzy ones by allowing fuzziness in the functional dependencies^[6, 7]. Many different proposals for fuzzy data models for databases can be found in^[8].

Investigations have also been made for the extension of relational query languages with fuzzy logic. For example, Takahashi^[9] proposes a fuzzy query language (FQL) based on the relational domain calculus^[10]. The language FQUERY by Kacprzyk and Zadrozny^[11] uses fuzzy terms and has been implemented as a prototype in the Microsoft product Access.

In our work on a fuzzy classification and a fuzzy classification query language FCQL (fuzzy classification query language), we choose a slightly different research direction, originally indicated by Schindler^[12]: we limit ourselves to an extension of the relational database schema by creating a context model for propose fuzzy classification of table contents. Based on this, we develop the language FCQL, which allows fuzzy queries to the database schema using predefined linguistic variables and transmits them to the underlying (sharp) database in SQL calls. In this way, we avoid migrating the database to a fuzzy database at great expense^[13] or confronting the user with fuzzy SQL^[14]. Fuzzy predicates would lead to a variety of semantic effects and a user would have to make different interpretations. With FCQL, on the other hand, we give the user a data mining tool so that he can start extended queries and calculate improved decision-making bases based on a predefined fuzzy classification of his data stocks.

Context model and classification

Extensive databases are often confusing and therefore difficult to analyze and evaluate. In order to obtain meaningful information, the user must restructure and, if necessary, condense their stocks. To this end, various methods and concepts for building and operating a data warehouse have been developed. There are also data mining tools to gain new insights from the databases.

We choose a context model approach to be able to specify classes in the relational database schema. For the analysis and evaluation of a large number of suppliers, for example, it makes sense to group suppliers that are as similar as possible into classes. You then get the set of "suppliers with quality problems" or the set of "suppliers with whom the business relationship should be expanded" as an example. Such a combination of suppliers into classes means a reduction in complexity. The user can thus maintain and analyze his supplier relationships more clearly, thanks to the reduced flood of data.

In addition, important characteristics of the suppliers are made visible through the classification. This additional knowledge allows the user to analyze entire classes in a targeted and holistic manner and to work out the relationships between different classes.

When classifying objects in a relational database, a distinction can be made between sharp and fuzzy methods. In the case of a strict classification, the database objects are assigned to the class in a dichotomous manner, i.e. the set membership function of the object to the class is 0 for not included or 1 for included. A classic procedure would therefore assign a supplier to the "Suppliers with quality problems" class or the "Suppliers with whom the business relationship should be expanded" class. A fuzzy procedure, on the other hand, allows values between 0 and 1 for the quantity membership function: A supplier can, for example, belong to the class "suppliers with quality problems" with a value of 0.3 and at the same time to the class "suppliers with whom the business relationship has been developed" with a membership of 0.7 should be". A fuzzy classification therefore enables a differentiated interpretation of the class affiliation; with database objects of a class, one can distinguish between peripheral and core objects, and database objects can also belong to two different classes at the same time.

In the fuzzy-relational data model with contexts - in short, in the context model - a context is assigned to each attribute A_j , defined on a value range $D(A_j)$. A context $C(A_j)$ is a partition of $D(A_j)$ into equivalence classes. A relational database schema with contexts therefore consists of a set of attributes $A=(A_1, \dots, A_n)$ and a set of associated contexts $C=(C_1(A_1), \dots, C_n(A_n))$ according to [15].

Material-specific data on the delivered quality and the delay should be recorded for an evaluation of suppliers. The corresponding database schema $lfb(A, C)$ for supplier evaluation is with the attributes.

$A = (\text{supplier, material, quality, delay})$ and the contexts $K = (C(\text{supplier}), C(\text{material}), C(\text{quality}), C(\text{delay}))$

Specified. The material quality is described with the terms $D(\text{quality}) = \{\text{high, medium, sufficient, low}\}$. The delay is the delay that has occurred so far compared to the promised delivery date in days. The following partitions apply to the contexts:

- $C(\text{supplier}) = \{\{\text{supplier names}\}\}$
- $C(\text{material}) = \{\{\text{material identification numbers}\}\}$
- $C(\text{quality}) = \{\{\text{high, medium}\}, \{\text{sufficient, low}\}\}$
- $C(\text{delay}) = \{\{1, 2, 3, 4, 5\}, \{6, 7, 8, 9, 10\}\}$

The contexts $C(\text{supplier})$ and $C(\text{material})$ consist of the broadest equivalence classes that correspond to the respective value ranges. According to $C(\text{quality})$, it is assumed for the evaluation of a query, for example, that the quality levels "sufficient" and "low" are equivalent. In

addition, $C(\text{delay})$ means that the distinction between a delay of e.g. one day and five days is irrelevant for queries. In Figure 2 we show the classification space for our simple example of supplier evaluation. By partitioning the value ranges of quality and delay, we get the four equivalence classes C_1, C_2, C_3 and C_4 . The meaning of the content of the classes is made visible by semantic class names; e.g. for class C_4 the name "Check relationship" is chosen. An orientation to the equivalence classes facilitates a meaningful interpretation.

D(delay)	10	C2		C4	
	9	delay admonish		check relationship	
	8				
	7				
	6				
	5	C1		C3	
	4	expand relationship		discuss quality	
	3				
	2				
	1				
	high	medium	sufficient	low	
D(quality)					

Fig 2: Classification space spanned by the characteristics of quality and delay

It is one of the tasks of the database administrator to define suitable equivalence classes in cooperation with the relevant specialists.

In a classification, the selected features must be independent. To do this, it may be necessary to analyze the data and calculate the correlation coefficients between the characteristics. Another clue to dependent characteristics comes from uncovering transitive dependencies in database design.

Context redundant tuples

In the relational model, one speaks of redundant tuples or tables if there are multiple occurrences in the tuple components that could be deleted without loss of information. The theory of normal forms was developed for the preservation of redundancy-free relations [16, 10]. The redundancy of two tuples in the context model is softer defined: Two tuples t and t' are called context-redundant if all tuple components t_i and t'_i belong to the same equivalence class. Context-redundancy-free relations are obtained by mixing operations, which are discussed in more detail below.

A database object belongs to a class if its feature vector points to the corresponding subdomain. In the presented context model, the set-theoretic unification as a mixing operation is chosen as the classification function. This operation is performed when evaluating an expression of context-based relational algebra in order to obtain context-redundancy-free result relations [17, 12].

Let's look at an example: The suppliers shown in Figure 3 are to be evaluated for material 802.025. Objects are the individual vendors identified by the vendor attribute of the composite primary key. The characteristics relevant for an evaluation are quality and delay. A classification of the suppliers for material 802.025 provides the following combination of context-based projection Π and selection Σ . The operators of the context-based relational algebra are

expressed using Greek capital letters, based on the work of Schenoi [17].

lfb	supplier	material	quality	Schedule delay
	BAW	802.025	sufficient	8
	DEWAG	802.025	medium	5
	DEWAG	809.200	high	8
	KBA	802.025	sufficient	7
	KBA	809.025	sufficient	3
	MD	840.024	low	9
	MD	802.025	sufficient	8
	MTX	809.200	medium	2
	MTX	809.200	high	4
	MAM	802.025	high	7
	MAM	840.024	low	6
	ZT	802.025	high	8
	ZT	840.024	medium	2

Fig 3: Table LFB for supplier evaluation

For the evaluation of the query, the context C(Material) is replaced by the precise context PC(Material) = {{802.025},{809.200},...}. The result of the query is the context-redundancy-free, imprecise relation LFE in Figure 4, which results in a clear assignment of the objects Supplier to the classes C1 and C4 in the column of the object-identifying characteristic Supplier.

lfb	supplier	quality	delay
	MTX(Dewag)	{high, medium}	{2,5}
	{KBA, MAM, BAW, MD}	{sufficient, low}	{7,8}

Class: C1: expand relationship, C4: check relationship

Fig 4: Clear allocation of suppliers to classes C1 and C4

A material-independent evaluation of the suppliers shows that the evaluation of a query with the context model does not always produce results in the sense of a sharp classifier. For this we consider the following context-based projection of the relation lfb:

$$[Supplier, Quality, Delay, C()](lfb)[[$$

The result table lfs in Figure 5 illustrates that only the suppliers BAW and MTX were sharply classified. On the other hand, for example, the vendor MD was assigned to class C1 and C4. This means that the merge operation for the supplier MD currently still delivers a contradictory

recommendation, namely "expand relationship" (C1) and "check relationship" (C4). The evaluation of a query in the context model does not generally assign a database object to one and only one class.

lfb	supplier	quality	delay
	{MTX, ZT, MD, Dewag}	{high, medium}	{2, 4, 5}
	{MAM, Dewag, ZT}	{high, medium}	{6, 8}
	{KBA}	{sufficient}	{3}
	{KBA, MAM, BAW, MD}	{sufficient, low}	{7, 8, 9}

Class: C1: expand relationship, C2: Request delay, C3: Discuss quality, C4: Check relationship

Fig 5: Fuzzy assignment of suppliers to classes (except BAW and MTX)

The multiple assignment of database objects to classes can lead to conflicting recommendations for action. In order to reduce this uncertainty, the context model is further developed into a fuzzy classification using elements from the theory of fuzzy sets.

Fuzzy classification with linguistic variables

Classes represent different states for a specific database object. In the case of multiple assignments of an object to different classes, it is not possible to make a clear distinction between the different states. In order to be able to derive fuzzy classes from the sharp contexts considered so far, verbal terms are first assigned to the equivalence classes. An idea of the elements belonging to the equivalence class with a fuzzy assignment is then connected with these concepts.

A formal description of the assignment of verbal terms to equivalence classes is possible with the concept of linguistic variables [18]. Linguistic variables do not have numbers or distributions as values, but rather linguistic constructs or Terms (verbal terms). The content of these terms is defined by fuzzy sets on a so-called basis variable. As an example, Figure 6 shows the definition of the characteristic delay as a linguistic variable based on the basic variable "cumulative delay". The domain of definition of the basic variable is equal to the domain of values D(delay). The linguistic variable has the term set T(delay) = {acceptable, unacceptable} with the verbal terms "acceptable" and "unacceptable" to describe the two equivalence classes {1, 2, 3, 4, 5} resp. {6, 7, 8, 9, 10}.

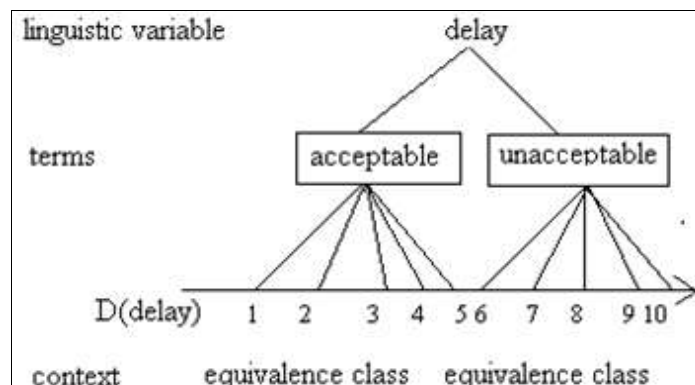


Fig 6: Assignment of verbal terms to equivalence classes

The semantic description of fuzzy classes with linguistic variables makes it possible to accommodate human understanding. Each term is represented by a fuzzy set

defined by membership functions on the domains of the attributes. The vague terms describing the equivalence classes are the labels of the fuzzy sets. In Figure 7, a

lateness is simultaneously “acceptable” and “unacceptable” to the degree of 0.5, i.e. the belonging of 5 days to the sharp quantities $\mu_{\text{acceptable}}$ and $\mu_{\text{unacceptable}}$ is 0.5. A schedule delay of

5 days is therefore not exclusively acceptable or unacceptable as with sharp classes.

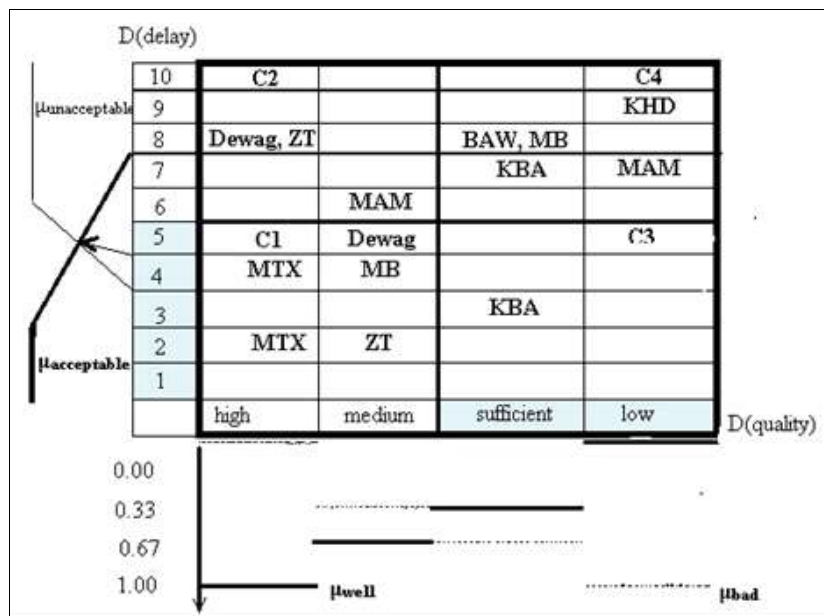


Fig 7: Fuzzy partitioning of the value ranges with membership functions

The description of the vague terms "acceptable" and "unacceptable" with the membership functions $\mu_{\text{acceptable}}$ and $\mu_{\text{unacceptable}}$ causes the value range $D(\text{delay})$ to be partitioned indistinctly. Similarly, the range of values $D(\text{quality})$ is divided by the terms "good" and "bad". This results in classes with continuous transitions, i.e. fuzzy classes, in the context model.

The class affiliation of an object results from the affiliation of the tuple components (characteristic values) to the fuzzy sets whose labels describe the class. The object affiliation of MTX, e.g. with the feature vector (4, high) related to the term "acceptable" of the feature delay corresponds to the affiliation value.

$$M(\text{MTX}|\text{acceptable}) = \mu_{\text{acceptable}} \quad (4)$$

The affiliation $M(O_i|C_k)$ of an object O_i to the class C_k results from the aggregation over all terms of the linguistic variables that define the class. Class C1, for example, is described by the terms "acceptable" and "good". The aggregation must therefore correspond to a conjunction of the individual membership values. Various operators have been developed for this in the theory of fuzzy sets, see e.g. [18]. A general class of operators are the triangular operators or t-norms with the minimum operator as an example. The membership of $\text{MTX}(4, \text{high})$ in the class C1 is with this operator

$$M(\text{MTX}(4, \text{high})|C1) = \min\{ \mu_{\text{acceptable}}(4), \mu_{\text{well}}(\text{high}) \}$$

The use of the minimum operator as an aggregation operator means that the characteristic with the lowest membership value is decisive for determining whether an object belongs to a class. When classifying suppliers, a supplier is acceptable in terms of its delay in delivery, but delivers poor quality. An aggregation with the minimum operator would only classify the supplier as a “poor” supplier because of its quality. If, on the other hand, the supplier evaluation takes

place through human consideration, then one would make a certain compensation between poor quality and acceptable delay. In other words, in many cases poor quality will not be the only criterion when ranking a supplier.

Human decision-making behavior is often characterized by compensatory considerations. For this purpose, special operators such as the compensatory and or the so-called γ -operator were developed in fuzzy logic [18, 31]. The fuzzy result relation l_{fu} from Figure 8, in which the tuple components are fuzzy sets, shows a classification result with an aggregation via the γ -operator.

l_{fu}	supplier	quality	delay
	{ (MTX, 1.00), (ZT, 0.45), (MD, 0.45), (Dewag, 0.35) }	well	acceptable
	{ (MAM, 0.40), (Dewag, 0.65), (ZT, 0.55) }	well	unacceptable
	{ (KBA, 0.31) }	bad	acceptable
	{ (KBA, 0.69), (MAM, 0.60), (BAW, 1.00), (MD, 0.55) }	bad	unacceptable

C1: expand relationship, C2: remind appointment
C3: discuss quality, C4: check relationship

Fig 8: Fuzzy classes by compensatory aggregation with the γ -operator

The fuzzy quantities in the Supplier column show the fuzzy decomposition. For example, the supplier Dewag has an affiliation of 0.35 to the class "expand relationship" (C1) and 0.65 to the class "admonishment of delay" (C2). In the sharp classification of table l_{fs} from Figure 5, on the other hand, Dewag was assigned to the classes "expand relationship" and "remind delay" with the affiliation 1.0. A comparison with the result from Figure 8 illustrates that the supplier Dewag is more concerned with scheduling problems and not quality issues. The uncertainty regarding the maintenance of the relationship with the supplier is thus clarified.

Language FCQL for fuzzy classification

In our work, we refrain from developing fuzzy query languages on the basis of a context-based relational algebra or a fuzzy domain calculus, as variously proposed and

partially implemented [11, 15, 19]. Our language approach is limited to a classification language called FCQL, which can be used to define and query fuzzy classes. Specifically, we use SQL on the underlying sharp databases to then generate

a fuzzy result relation. To do this, it is necessary to use SQL statements to select and aggregate context-redundant tuples from the sharp database.

query language	example	Query type in the context model
SQL	select supplier from lfb where delay = 4	sharp query through precise contexts with single element equivalence class
MIQUEL	select supplier from lfb where delay approx=4	fuzzy query through sharp contexts with multi-element equivalence class
fCQL	classify supplier from lfb classify supplier from lfb with class is appointment problem classify supplier from lfb with delay is acceptable and quality is good	fuzzy classification through vague contexts with fuzzy equivalence classes

Fig 9: Overview of context-based language approaches for relational

In their work, Finnerty and Shenoï [14] designed the query language MIQUEL in order to be able to direct fuzzy queries to a relational database. A MIQUEL query differs from an ordinary SQL query in the where clause select features from tables where selection condition with context designation.

According to Finnerty and Shenoï, the simplest form of a contextual condition is an expression of the form

>attribute> <context> <reoperator> <expression<

e.g. in Figure 9 the condition "delay approximately = 4". In other words, with the MIQUEL language suggestion, the query condition always consists of a sharp target value and optionally a context. The MIQUEL language thus permits sharp and fuzzy queries at the same time.

In contrast to MIQUEL, classification queries with the language FCQL [20] operate on the linguistic level with vague contexts. This has the advantage that the user does not need to know a specific target value or context, just the column name of the object-identifying feature and the table or view that contains the feature values. For a targeted view of individual classes, the user can specify a class or specify features with a verbal description of their characteristics. Classification queries therefore work with verbal descriptions at the feature and class level:

Classify object

From Table with classification condition

The FCQL language is based on SQL, with the projection list in the select clause being replaced by the column name of the object to be classified.

While the where clause in SQL contains a selection condition, we use the with clause to describe the classification condition.

As an example of an FCQL query, "classify supplier from lfb" generates a classification of all suppliers in table lfb (from Figure 3). A specific class is queried with "classify supplier from lfb with class is appointment problem". If one dispenses with the definition of the class, one can select a specific set of objects with the linguistic descriptions of the equivalence classes. As an example, consider the query "classify supplier from lfb with delay is acceptable and quality is good". This query consists of the identifier of the object to be classified (supplier), the name of the basic table

(lfb), the critical characteristic names (delay or quality) and the names of the predefined equivalence classes (acceptable or good).

Outlook

For code generation we had to extend the database schema with three descriptive tables for contexts, classes and membership functions. We have tested our implementation on an industry database. The responsible marketing department has a mature data Warehouse, but they want to further analyze and evaluate the customer and product inventories using methods of fuzzy logic. Thanks to the chosen approach with fuzzy classes, we didn't have to carry out a complex database migration to take over the data stock. With the field test, we hope that the classification language FCQL will complement the tool set for data mining and knowledge discovery in a meaningful way.

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